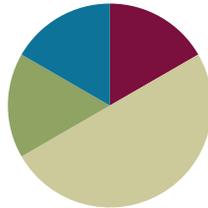


## Lesson 1

Objective: Understand *equal groups* of as multiplication.

### Suggested Lesson Structure

■ Fluency Practice	(10 minutes)
■ Application Problem	(10 minutes)
■ Concept Development	(30 minutes)
■ Student Debrief	(10 minutes)
<b>Total Time</b>	<b>(60 minutes)</b>



### Fluency Practice (10 minutes)

- Group Counting **3.OA.1** (10 minutes)

### Group Counting (10 minutes)

Note: Basic skip-counting skills from Grade 2 shift focus in this Grade 3 activity. Group-counting lays a foundation for interpreting multiplication as repeated addition. When students count groups in this activity, they add and subtract groups of two when counting up and down.

- T: Let's count to 20 forward and backward. Watch my fingers to know whether to count up or down. A closed hand means stop. (Show signals as you explain.)
- T: (Rhythmically point up until a change is desired. Show a closed hand then point down.)
- S: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 19, 18, 17, 16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1, 0.
- T: Let's count to 20 forward and backward again. This time whisper every other number. Say the other numbers in a regular voice.
- S: (Students whisper then speak every other number to 20 forward and backward.)
- T: Let's count to 20 forward and backward again. This time, hum every other number instead of whispering. As you hum, think of the number.
- S: (Hum), 2, (hum), 4, (hum), 6, etc.
- T: Let's count to 20 forward and backward again. This time, think every other number instead of humming.
- S: (Think), 2, (think), 4, (think), 6, etc.
- T: What did we just count by? Turn and talk to your partner.
- S: Twos.

- T: Let's count by twos. (Direct students to count forward to and backward from 20, changing directions at times.)

### Application Problem (10 minutes)

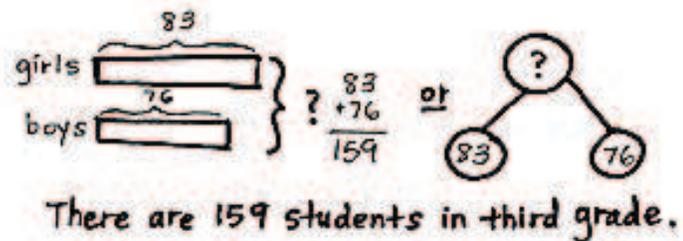
There are 83 girls and 76 boys in the third grade. How many total students are in the third grade?

Note: Students may choose to use a tape diagram or a number bond to model the problem. They are also likely to solve today's application problem in less than 10 minutes. Ten minutes have been allotted in order for you to review the RDW (Read, Draw, Write) procedure for problem-solving.

Directions on the Read, Draw, Write (RDW)

Process: Read the problem, draw and label, write a number sentence, and write a word sentence. The more students participate in reasoning through problems with a systematic approach, the more they internalize those behaviors and thought processes.

(Excerpted from "How to Implement A Story of Units.")



### Concept Development (30 minutes)

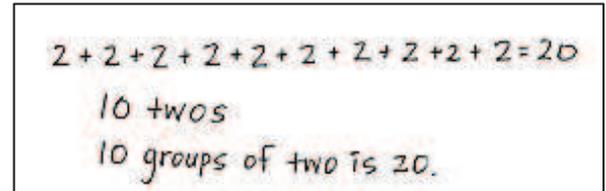
Materials: (S) 12 counters per student, personal white boards.

#### Problem 1: Skip-count to find the total number of objects.

- T: (Select 10 students to come to the front.) At the signal, say how many arms you have. (Signal.)
- S: 2 arms!
- T: Since we each represent a group of 2 arms, let's skip-count our volunteers by twos to find how many arms they have altogether. To keep track of our count, the students will raise up their arms when we count them.
- S: (Count 2, 4, 6...20.)
- T: How many raised arms do we have in all?
- S: 20.
- T: Arms down. How many twos did we count to find the total? Turn and whisper to your partner.
- S: 10 twos.
- T: What did you count to find the number of twos?
- S: I counted the number of students in the front because each person represents a group of two.
- T: Skip-count to find the total number of arms.

- S: (Students say 2, 4, 6.... As they count, write  $2 + 2 + 2...$ )
- T: Look at our addition sentence. Show thumbs up if you see the correct number of twos.
- S: (Show thumbs up.)
- T: (Under the addition sentence write 10 twos.) Clap your hands if you agree that 10 groups of two is 20.
- S: (Clap hands.)
- T: (Write '10 groups of two is 20' under the other expressions.)

Sample teacher board:



$2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 + 2 = 20$   
 10 twos  
 10 groups of two is 20.

**Problem 2: Understand the relationship between repeated addition, counting groups in unit form, and multiplication equations.**

Seat students at tables with personal white boards and 12 counters each.

- T: You have 12 counters. Use your counters to make **equal groups** of two. How many counters will you put in each group? Show with your fingers.
- S: (Students hold up 2 fingers and begin to make groups of two.)
- T: How many equal groups of two did you make? Tell at the signal. (Signal.)
- S: 6 groups.
- T: 6 equal groups of how many counters?
- S: 6 equal groups of 2 counters.
- T: 6 equal groups of 2 counters equal how many counters altogether?
- S: 12 counters.
- T: Write an addition sentence to show your groups on your personal white board.
- S: (Write  $2 + 2 + 2 + 2 + 2 + 2 = 12$ .)
- T: (Record the addition sentence on the board.) How many twos did we add to make 12?
- S: 6 twos.
- T: (Record 6 twos = 12 under the addition sentence.)  $6 \times 2$  is another way to write  $2 + 2 + 2 + 2 + 2 + 2$  or 6 twos. (Record  $6 \times 2 = 12$  under 6 twos = 12 on the board.) These number sentences are all saying the same thing. Another name for number sentence is **equation**.
- T: Turn and talk to your partner. How do you think  $6 \times 2 = 12$  relates to the other equations?

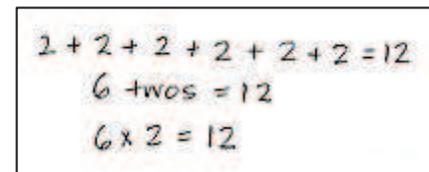


**NOTES ON MULTIPLE MEANS OF REPRESENTATION:**

For some classes it may be necessary to clearly connect the word *times* and the symbol  $\times$ . Have students analyze the model. "How many times do you see a group of three?" Have them count the groups, write the equation, and say the words together.

- "4 groups of three equals 12."
- "4 times three equals 12."

Sample teacher board:



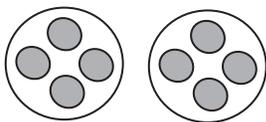
$2 + 2 + 2 + 2 + 2 + 2 = 12$   
 6 twos = 12  
 $6 \times 2 = 12$

- S: They all have twos in them and the answer is 12. → I think the 6 shows how many twos there are.  
 → You have to count two 6 times because there are 6 groups of them. That’s how you get 6 times 2.  
 →  $6 \times 2$  might be an easier way to write a long addition sentence.
- T: Ways that are easier and faster are efficient. When we have equal groups, **multiplication** is a more efficient way of showing the total than repeated addition.

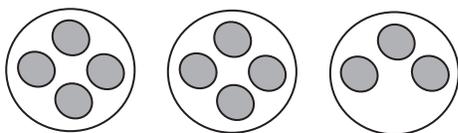
Repeat the process with 4 threes, 3 fours and 2 sixes with the objective of getting students comfortable with the relationship between repeated addition, counting groups in unit form, and multiplication equations. In this lesson avoid emphasis on finding solutions.

**Problem 3: Write multiplication sentences from equal groups.**

(Draw or project the following picture.)



- T: These are equal groups. Turn and tell your partner why they are equal.
- S: There is the same number of grey circles in each group.  
 → All of the grey circles are the same size and shape, and there are 4 in each group.
- T: Work with your partner to write a repeated addition and a multiplication sentence for this picture.
- S: (Write  $4 + 4 = 8$ , and either  $2 \times 4 = 8$  or  $4 \times 2 = 8$ .)
- T: (Project or draw the following image.) Look at my new drawing and the multiplication sentence I wrote to represent it. Check my work by writing an addition sentence and counting to find the total number of objects.



$3 \times 4 = 12$

- S: (Write  $4 + 4 + 3 = 11$ .)
- T: Use your addition sentence as you talk in partners about why you agree or disagree with my work.
- S: I disagree because my addition sentence equals 11, not 12. → It’s because that last group doesn’t have 4 circles. → You can do multiplication when the groups are equal. → Here the groups aren’t equal, so the drawing doesn’t show  $4 \times 3$ .
- T: I hear most students disagreeing because my groups are not equal. True, to **multiply** you must have equal groups.



**NOTES ON MULTIPLE MEANS OF ACTION AND EXPRESSION:**

Some students may need more scaffolding to realize that you can’t use multiplication to find the total amount of items in groups that are not equal. You might use the following questions to scaffold.

- “Does the drawing show groups of 4 modeled 3 times?”
- “Does 4 *times* 3 represent this drawing?”
- “How might we redraw the picture to make it show  $4 \times 3$ ?”
- 

MP.3

### Problem Set (10 minutes)

Students should do their personal best to complete the Problem Set within the allotted 10 minutes. Some problems do not specify a method for solving. This is an intentional reduction of scaffolding that invokes MP.5, Use Appropriate Tools Strategically. Students should solve these problems using the RDW approach used for Application Problems.

For some classes, it may be appropriate to modify the assignment by specifying which problems students should work on first. With this option, let the careful sequencing of the Problem Set guide your selections so that problems continue to be scaffolded. Balance word problems with other problem types to ensure a range of practice. Assign incomplete problems for homework or at another time during the day.

### Student Debrief (10 minutes)

**Lesson Objective:** Understand *equal groups of as* multiplication.

The Student Debrief is intended to invite reflection and active processing of the total lesson experience.

Invite students to review their solutions for the Problem Set. They should check work by comparing answers with a partner before going over answers as a class. Look for misconceptions or misunderstandings that can be addressed in the Debrief. Guide students in a conversation to debrief the Problem Set and process the lesson. You may choose to use any combination of the ideas below to lead the discussion.

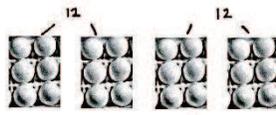
- On the first page, what did you notice about the answers to your problems?
- Discuss the relationship between repeated addition and the unit form *2 groups of three* or *3 groups of two*, depending on the drawing.
- 

NYS COMMON CORE MATHEMATICS CURRICULUM Lesson 1 Worksheet 3•1

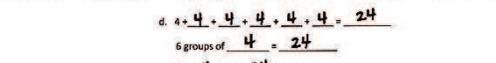
Name Gina Date 9/1

1. Fill in the blanks to make true statements.

  $3 \text{ groups of five} = \underline{15}$        $3 + 3 + 3 + 3 + 3 = \underline{15}$   
 $3 \text{ fives} = \underline{15}$        $5 \text{ groups of three} = \underline{15}$   
 $3 \times 5 = \underline{15}$        $5 \times 3 = \underline{15}$

  $6 + 6 + 6 + 6 = \underline{24}$   
 $\underline{4}$  groups of six =  $\underline{24}$   
 $4 \times \underline{6} = \underline{24}$

  $4 + 4 + 4 + 4 + 4 = \underline{20}$   
 $4 \times \underline{5} = \underline{20}$

  $4 + 4 + 4 + 4 + 4 + 4 = \underline{24}$   
 $6 \text{ groups of } \underline{4} = \underline{24}$   
 $6 \times \underline{4} = \underline{24}$

COMMON CORE Lesson 1: Interpret "Equal Groups of" as Multiplication Date: 4/24/13 engage<sup>ny</sup> 1.A.7

NYS COMMON CORE MATHEMATICS CURRICULUM Lesson 1 Worksheet 3•1

2. The picture below shows 2 groups of apples. Does the picture below show  $2 \times 3$ ? Explain why or why not.

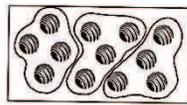


No, this picture does not show  $2 \times 3$ . There are 2 groups of apples, but they are not equal groups. It shows 1 group of 3 and 1 group of 2. You can also tell because there are 5 apples, not 6.

3. Draw a picture to show  $2 \times 3 = 6$ .



4. Caroline, Brian and Marta want to share a box of chocolates so that they each get the same amount. Circle the chocolates below to show 3 groups of 4. Then write addition and multiplication sentences to represent the problem.



$4 + 4 + 4 = 12$   
 $3 \times 4 = 12$

COMMON CORE Lesson 1: Understand "equal groups of" as multiplication Date: 4/24/13 engage<sup>ny</sup> 1.A.8

- Discuss the relationship between repeated addition, unit form, and the **multiplication equation**  $3 \times 2 = 6$ .
- Review the new vocabulary presented in the lesson, including **equal groups**, **multiply**.

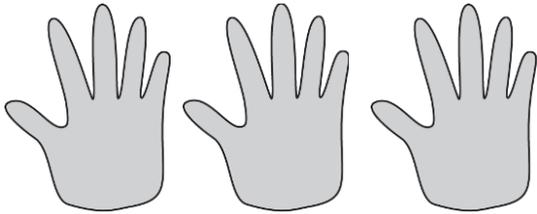
### Exit Ticket (3 minutes)

After the Student Debrief, instruct students to complete the Exit Ticket. A review of their work will help you assess the students' understanding of the concepts that were presented in the lesson today and plan more effectively for future lessons. You may read the questions aloud to the students.

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Fill in the blanks to make true statements.



a. 3 groups of five = \_\_\_\_\_

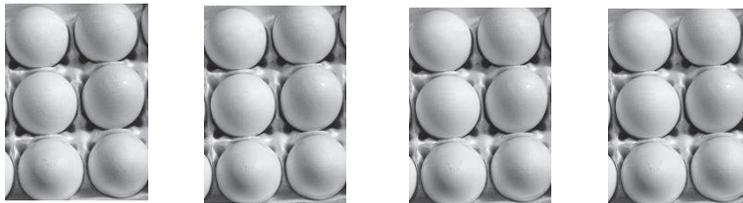
3 fives = \_\_\_\_\_

$3 \times 5 =$  \_\_\_\_\_

b.  $3 + 3 + 3 + 3 + 3 =$  \_\_\_\_\_

5 groups of three = \_\_\_\_\_

$5 \times 3 =$  \_\_\_\_\_



c.  $6 + 6 + 6 + 6 =$  \_\_\_\_\_

\_\_\_\_\_ groups of six = \_\_\_\_\_

$4 \times$  \_\_\_\_\_ = \_\_\_\_\_

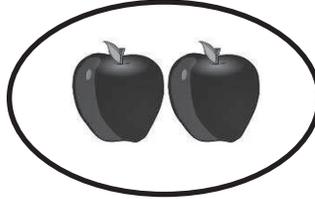
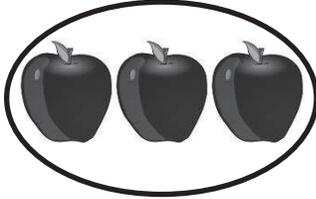


d.  $4 +$  \_\_\_\_\_  $+$  \_\_\_\_\_  $+$  \_\_\_\_\_  $+$  \_\_\_\_\_  $+$  \_\_\_\_\_  $=$  \_\_\_\_\_

6 groups of \_\_\_\_\_ = \_\_\_\_\_

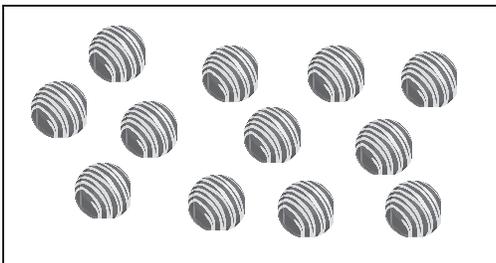
$6 \times$  \_\_\_\_\_ = \_\_\_\_\_

2. The picture below shows 2 groups of apples. Does the picture below show  $2 \times 3$ ? Explain why or why not.



3. Draw a picture to show  $2 \times 3 = 6$ .

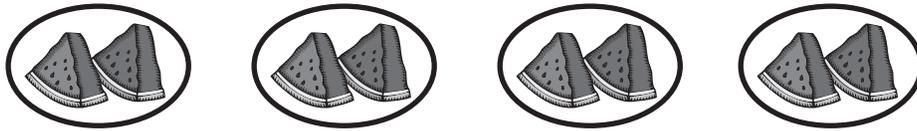
4. Caroline, Brian and Marta want to share a box of chocolates so that they each get the same amount. Circle the chocolates below to show 3 groups of 4. Then write addition and multiplication sentences to represent the problem.



Name \_\_\_\_\_

Date \_\_\_\_\_

1. The picture below shows 4 groups of 2 slices of watermelon. Write repeated addition and multiplication sentences to represent the picture.



$$2 + \underline{\quad} + \underline{\quad} + \underline{\quad} = \underline{\quad}$$

$$4 \times \underline{\quad} = \underline{\quad}$$

2. Draw a picture to show  $3 + 3 + 3 = 9$ . Then write a multiplication sentence to represent the picture.

Name \_\_\_\_\_

Date \_\_\_\_\_

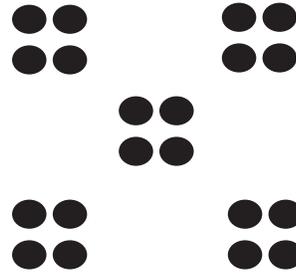
1. Fill in the blanks to make true statements.



a. 4 groups of five = \_\_\_\_\_

4 fives = \_\_\_\_\_

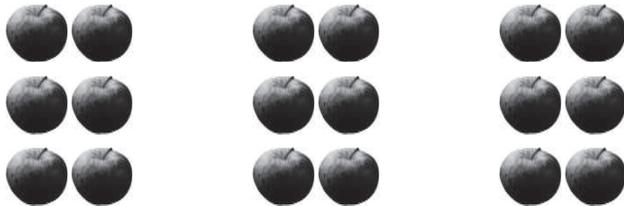
$4 \times 5 =$  \_\_\_\_\_



b. 5 groups of four = \_\_\_\_\_

5 fours = \_\_\_\_\_

$5 \times 4 =$  \_\_\_\_\_



c.  $6 + 6 + 6 =$  \_\_\_\_\_

\_\_\_\_\_ groups of six = \_\_\_\_\_

$3 \times$  \_\_\_\_\_ = \_\_\_\_\_



d.  $3 +$  \_\_\_\_\_  $+$  \_\_\_\_\_  $+$  \_\_\_\_\_  $+$  \_\_\_\_\_  $+$  \_\_\_\_\_  $+$  \_\_\_\_\_  $=$  \_\_\_\_\_

6 groups of \_\_\_\_\_ = \_\_\_\_\_

$6 \times$  \_\_\_\_\_ = \_\_\_\_\_

2. The picture below shows 3 groups of hot dogs. Does the picture below show  $3 \times 3$ ? Explain why or why not.



3. Draw a picture to show  $4 \times 2 = 8$ .

4. Circle the pencils below to show 3 groups of 6. Write addition and multiplication sentences to represent the problem.

